

## § 6.1 Composite Functions

### Composition of Functions:

If  $f$  and  $g$  are functions, then the composite function or composition, of  $g$  and  $f$  is:

$$(g \circ f)(x) = g[f(x)] \quad (\text{Note: this is read "g of f of x".})$$

for all  $x$  in the domain of  $f$  such that  $f(x)$  is in the domain of  $g$ .

Example 1: Let  $f(x) = x^2 + 3x - 1$  &  $g(x) = 2x + 3$

Find  $(f \circ g)(x)$  and  $(g \circ f)(x)$ .

Example 2: Let  $f(x) = 2x^2 - 3$  and  $g(x) = 4x$

Find  $(f \circ g)(1)$  and  $(g \circ f)(1)$  and  $(f \circ f)(-2)$ .

## Show That Two Composite Functions Are Equal

Example 3:

$$\text{If } f(x) = 3x - 4 \text{ and } g(x) = \frac{1}{3}(x + 4)$$

Show that  $(f \circ g)(x)$  and  $(g \circ f)(x) = x$