

$$h = \frac{-b}{2a} \quad k = f(h)$$

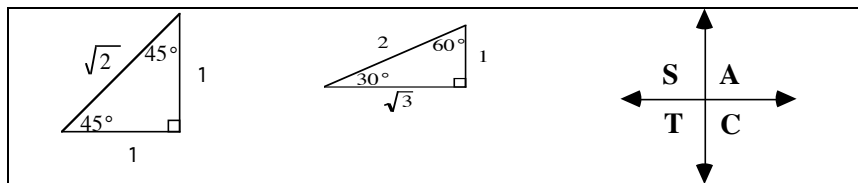
$$K = \frac{1}{2}bc \sin A = \frac{1}{2}ab \sin C = \frac{1}{2}ac \sin B$$

$$\frac{\pi}{180}$$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$s = r\theta$$

**sohcahtoa**



$$\begin{array}{lll} \sin \theta = \frac{1}{\csc \theta} & \cos \theta = \frac{1}{\sec \theta} & \tan \theta = \frac{1}{\cot \theta} \\ \csc \theta = \frac{1}{\sin \theta} & \sec \theta = \frac{1}{\cos \theta} & \cot \theta = \frac{1}{\tan \theta} \end{array}$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta} \quad \cot \theta = \frac{\cos \theta}{\sin \theta}$$

$$\sin^2 \theta + \cos^2 \theta = 1 \quad \tan^2 \theta + 1 = \sec^2 \theta \quad 1 + \cot^2 \theta = \csc^2 \theta$$

### Sum or Difference of Two Angles Identities

$$\begin{array}{ll} \cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta & \tan(\alpha + \beta) = \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta} \\ \cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta & \\ \sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta & \tan(\alpha - \beta) = \frac{\tan \alpha - \tan \beta}{1 + \tan \alpha \tan \beta} \\ \sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta & \end{array}$$

### Double-Angle Identities

$$\begin{array}{ll} \sin 2\alpha = 2 \sin \alpha \cos \alpha & \\ \cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha & \tan 2\alpha = \frac{2 \tan \alpha}{1 - \tan^2 \alpha} \\ = 1 - 2 \sin^2 \alpha & \\ = 2 \cos^2 \alpha - 1 & \end{array}$$

### Half-Angle Identities

$$\begin{array}{l} \sin \frac{\alpha}{2} = \pm \sqrt{\frac{1 - \cos \alpha}{2}} \quad \tan \frac{\alpha}{2} = \frac{\sin \alpha}{1 + \cos \alpha} = \frac{1 - \cos \alpha}{\sin \alpha} \\ \cos \frac{\alpha}{2} = \pm \sqrt{\frac{1 + \cos \alpha}{2}} \end{array}$$

$$\begin{array}{lll} a^2 = b^2 + c^2 - 2bc \cos A & \text{OR} & \cos A = \frac{b^2 + c^2 - a^2}{2bc} \\ b^2 = a^2 + c^2 - 2ac \cos B & \text{OR} & \cos B = \frac{a^2 + c^2 - b^2}{2ac} \\ c^2 = a^2 + b^2 - 2ab \cos C & \text{OR} & \cos C = \frac{a^2 + b^2 - c^2}{2ab} \end{array}$$

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)} \quad \text{where } s = \frac{1}{2}(a+b+c).$$

**Generalized Formulas for Graphs**

$$y = a \sin(bx - c) + d \qquad y = a \csc(bx - c) + d$$

$$y = a \cos(bx - c) + d \qquad y = a \sec(bx - c) + d$$

$$y = a \tan(bx - c) + d \qquad y = a \cot(bx - c) + d$$

amplitude = $ a $	Inverse Functions (Restrictions)
period $\frac{\pi}{b}$ or $\frac{2\pi}{b}$	$y = \arctan x$ $-\infty < x < \infty$ $-\frac{\pi}{2} < y < \frac{\pi}{2}$
tick marks $\frac{\text{period}}{4}$	$y = \arcsin x$ $-1 \leq x \leq 1$ $-\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$
endpoints $bx - c = 0$ and $bx - c = \pi$ $bx - c = 0$ and $bx - c = 2\pi$ $bx - c = \frac{-\pi}{2}$ and $bx - c = \frac{\pi}{2}$	$y = \arccos x$ $-1 \leq x \leq 1$ $0 \leq y \leq \pi$
vertical shift = $d$	

**Product to Sum Identities**

$$\sin \alpha \cos \beta = \frac{1}{2} [\sin(\alpha + \beta) + \sin(\alpha - \beta)]$$

$$\cos \alpha \cos \beta = \frac{1}{2} [\cos(\alpha + \beta) + \cos(\alpha - \beta)]$$

$$\sin \alpha \sin \beta = \frac{1}{2} [\cos(\alpha - \beta) - \cos(\alpha + \beta)]$$

$$\cos \alpha \sin \beta = \frac{1}{2} [\sin(\alpha + \beta) - \sin(\alpha - \beta)]$$

**Sum-to-Product Identities**

$$\sin x + \sin y = 2 \sin\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right)$$

$$\sin x - \sin y = 2 \cos\left(\frac{x+y}{2}\right) \sin\left(\frac{x-y}{2}\right)$$

$$\cos x + \cos y = 2 \cos\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right)$$

$$\cos x - \cos y = -2 \sin\left(\frac{x+y}{2}\right) \sin\left(\frac{x-y}{2}\right)$$