§7.5 Graphs of the Other Trigonometric Functions
Graph of $\mathbf{y}=\boldsymbol{\operatorname { t a n }} \mathbf{x}$

| x | $\frac{-\pi}{2}$ | $\frac{-\pi}{4}$ | 0 | $\frac{\pi}{4}$ | $\frac{\pi}{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\tan \mathrm{x}$ | undefined | -1 | 0 | 1 | undefined |


since the domain of $y=\tan x$ is all real numbers except $\frac{(2 n+1) \pi}{2}$,the graph repeats infinitely to the left and the right
one period (or cycle) of the graph is on $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$
Example 1: Graph
a) $y=\tan \frac{x}{2}$
b) $y=-3 \tan 2 x$

## Graph of $y=\cot x$

| x | 0 | $\frac{\pi}{4}$ | $\frac{\pi}{2}$ | $\frac{3 \pi}{4}$ | $\pi$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\cot \mathrm{x}$ | undefined | 1 | 0 | -1 | undefined |


since the domain of $y=\cot x$ is all real numbers except $n \pi$, the graph repeats infinitely to the left and the right
one period (or cycle) of the graph is on $[0, \pi]$

Example 2: $\quad$ Graph $y=2 \cot \frac{x}{3}$

Graph of $y=\csc (x)$

| x | 0 | $\frac{\pi}{2}$ | $\pi$ | $\frac{3 \pi}{2}$ | $2 \pi$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{y}=\csc \mathrm{x}$ | undefined | 1 | undefined | -1 | undefined |


since the domain of $y=\csc x$ is all real numbers except $n \pi$, the graph repeats infinitely to the left and the right
one period (or cycle) of the graph is on $[0,2 \pi]$

## Graph of $\mathbf{y}=\sec (\mathbf{x})$

| x | 0 | $\frac{\pi}{2}$ | $\pi$ | $\frac{3 \pi}{2}$ | $2 \pi$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{y}=\sec \mathrm{x}$ | 1 | undefined | -1 | undefined | 1 |


since the domain of $y=\sec x$ is all real numbers except $\frac{(2 \mathrm{n}+1) \pi}{2}$, the graph repeats infinitely to the left and the right
one period (or cycle) of the graph is on $[0,2 \pi]$

Example 3: Graph a) $y=2 \csc \left(x+\frac{\pi}{4}\right) \quad$ b) $y=\sec (2 x)$

Example: $y=\tan \left(\frac{x}{2}\right)$

Formulas for General Form $y=a \tan (b x-c)+d$

| amplitude $=$ none | tick mark calculations: |
| :---: | :---: |
| period $($ of tan and cot $)=$ | (1) $-\pi$ <br> (2) $-\pi+\frac{\pi}{2}=\frac{-\pi}{2}$ |
| $\frac{\pi}{b}=\frac{\pi}{1 / 2}=2 \pi$ | (3) $\frac{-\pi}{2}+\frac{\pi}{2}=0$ <br> (4) $0+\frac{\pi}{2}=\frac{\pi}{2}$ |
| $\text { tick marks }=\frac{\text { period }}{4}=\frac{2 \pi}{4}=\frac{\pi}{2}$ | (5) $\frac{\pi}{2}+\frac{\pi}{2}=\pi$ |
| endpoints Solve: $\begin{array}{ll} b x-c=\frac{-\pi}{2} & b x-c=\frac{\pi}{2} \\ \frac{x}{2}=\frac{-\pi}{2} & \frac{x}{2}=\frac{\pi}{2} \\ x=-\pi & x=\pi \\ \text { (starts) } & \text { (ends) } \end{array}$ | $\begin{aligned} y= & \tan \left(\frac{x}{2}\right) \\ & 1 \tan \left(\frac{1}{2} x-0\right)+0 \end{aligned}$  |
| vertical shift $=$ none |  |

Example: $y=2 \cot \left(\frac{x}{3}\right)$
(Remember APTEV)

Formulas for General Form $\quad y=a \cot (b x-c)+d$

| amplitude $=$ none | tick mark calculations: |
| :---: | :---: |
|  | (1) 0 |
| period $($ of tan and cot $)=$ | (2) $0+\frac{3 \pi}{4}=\frac{3 \pi}{4}$ |
| $\frac{\pi}{b}=\frac{\pi}{1 / 3}=3 \pi$ | (3) $\frac{3 \pi}{4}+\frac{3 \pi}{4}=\frac{3 \pi}{2}$ |
|  | (4) $\frac{3 \pi}{2}+\frac{3 \pi}{4}=\frac{9 \pi}{4}$ |
| $\text { tick marks }=\frac{\text { period }}{4}=\frac{3 \pi}{4}$ | (5) $\frac{9 \pi}{4}+\frac{3 \pi}{4}=3 \pi$ |
| endpoints Solve: | $y=2 \cot \left(\frac{x}{3}\right)$ |
| $b x-c=0 \quad b x-c=\pi$ | $2 \cot \left(\frac{1}{3} x-0\right)+0$ |
| $\frac{x}{x}=0 \quad \underline{x}=$ | $a \times \mathrm{n}^{\text {b }}$, |
| $\overline{3}=0 \quad \overline{3}=\pi$ | $\begin{aligned} & y \\ & 2+0 \end{aligned}$ |
| $\mathrm{x}=0 \quad \mathrm{x}=3 \pi$ | , |
| (starts) (ends) | $0 \frac{3 \pi}{4} \frac{3 \pi}{2} \frac{4 \pi}{4} 3$ |
| vertical shift $=$ none |  |

Example: $\mathrm{y}=2 \csc \left(\mathrm{x}+\frac{\pi}{4}\right)$
(Remember APTEV)

Formulas for General Form $y=a \sin (b x-c)+d$ and $y=a \cos (b x-c)+d$

| $\text { amplitude }=\|a\|=\|2\|=2$ <br> period $($ of sine and cosine $)=$ $\frac{2 \pi}{\mathrm{~b}}=\frac{2 \pi}{1}=2 \pi$ $\text { tick } \text { marks }=\frac{\text { period }}{4}=\frac{2 \pi}{4}=\frac{\pi}{2}$ | tick mark calculations: <br> (1) $\frac{-\pi}{4}$ <br> (2) $\frac{-\pi}{4}+\frac{\pi}{2}=\frac{\pi}{4}$ <br> (3) $\frac{\pi}{4}+\frac{\pi}{2}=\frac{3 \pi}{4}$ <br> (4) $\frac{3 \pi}{4}+\frac{\pi}{2}=\frac{5 \pi}{4}$ <br> (5) $\frac{5 \pi}{4}+\frac{\pi}{2}=\frac{7 \pi}{4}$ |
| :---: | :---: |
| $\begin{array}{lc} \hline \text { endpoints } & \text { Solve: } \\ \mathrm{bx}-\mathrm{c}=0 & \mathrm{bx}-\mathrm{c}=2 \pi \\ \mathrm{x}+\frac{\pi}{4}=0 & \mathrm{x}+\frac{\pi}{4}=2 \pi \\ \mathrm{x}=\frac{-\pi}{4} & \mathrm{x}=2 \pi-\frac{\pi}{4}=\frac{7 \pi}{4} \\ \text { (starts) } & \text { (ends) } \end{array}$ |  |
| vertical shift $=\mathrm{d}=$ none |  |

Example: $y=\sec (2 x)$
Formulas for General Form $\mathrm{y}=\mathrm{a} \sin (\mathrm{bx}-\mathrm{c})+\mathrm{d}$ and $\mathrm{y}=\mathrm{a} \cos (\mathrm{bx}-\mathrm{c})+\mathrm{d}$


