

## §8.5 Double-Angle and Half –Angle Formulas

**REMEMBER YOU KNOW ALGEBRA !**

### Double-Angle Identities

$$\sin 2\alpha = 2 \sin \alpha \cos \alpha$$

$$\tan 2\alpha = \frac{2 \tan \alpha}{1 - \tan^2 \alpha}$$

$$\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha$$

$$= 1 - 2 \sin^2 \alpha$$

$$= 2 \cos^2 \alpha - 1$$

### Half-Angle Identities

$$\sin \frac{\alpha}{2} = \pm \sqrt{\frac{1 - \cos \alpha}{2}}$$

$$\tan \frac{\alpha}{2} = \frac{\sin \alpha}{1 + \cos \alpha} = \frac{1 - \cos \alpha}{\sin \alpha}$$

$$\cos \frac{\alpha}{2} = \pm \sqrt{\frac{1 + \cos \alpha}{2}}$$

Where the + or – sign is determined by the quadrant of the angle  $\frac{\alpha}{2}$ .

Example 1 Evaluate.      Find  $\sin 2\theta$ ,  $\cos 2\theta$ ,  $\tan 2\theta$

from  $\sin \theta = \frac{3}{5}$ ,     $\frac{\pi}{2} < \theta < \pi$

Example 2      Find the exact value.       $\cos 15^\circ$

Example 3     If  $\cos \alpha = \frac{-3}{5}$ ,      $\pi < \alpha < \frac{3\pi}{2}$ ,

find the exact value of;

a)  $\sin \frac{\alpha}{2}$

b)  $\cos \frac{\alpha}{2}$

c)  $\tan \frac{\alpha}{2}$