

Section 1.1
Limits and Graphs

Function Notation $f(x) = x^2 + 3x + 5$

f is the name of the function

f(x) indicates that x is the variable

f(x) is another name for y

f(2) means to plug in 2 for the variable x

$f(2) =$

f(2) is the y-value when x-value is 2

the point on the graph is

Limit Notation

→ means approaches, gets closer to

$x \rightarrow 3$ means as x approaches 3

$x \rightarrow 3^+$ means as x approaches 3 from the _____

$x \rightarrow 3^-$ means as x approaches 3 from the _____

Definition

As x approaches a, the limit of f(x) is L written

If all values of f(x) are close to L for all values of x that are sufficiently close to a. The limit L, if it exists, must be a unique real number.

Theorem

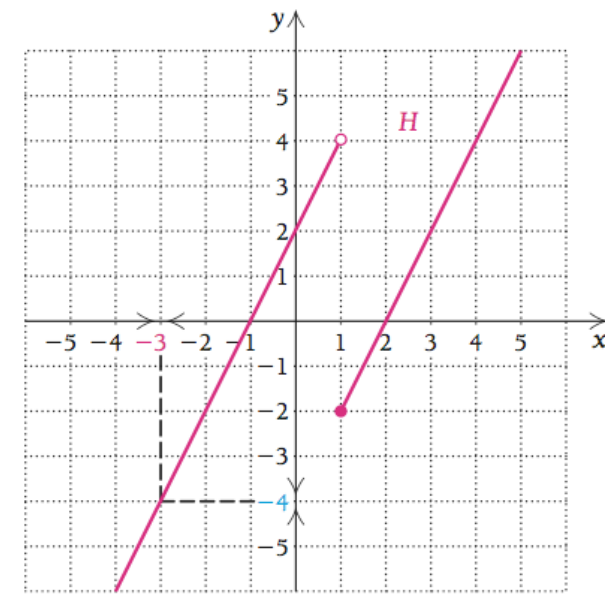
As x approaches a, the limit of f(x) is L if the limit from the _____ exists and the limit from the _____ exists and both numbers are equal.

If the right and left limits are not the same, THE limit _____

If $f(x)$ is increasing without bound, limit is _____.

If $f(x)$ is decreasing without bound, limit is _____.

Limits can also be used to describe behavior on the extreme _____ and _____ ends of graph.



Example 1:

Using the graph, find the following.

$$f(-3)$$

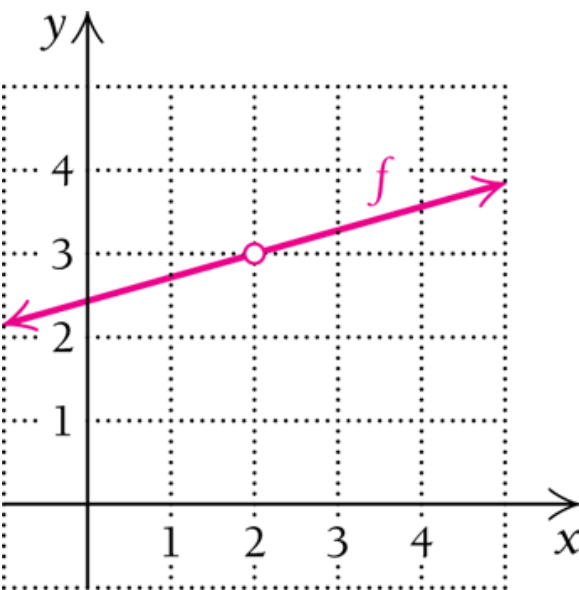
$$f(0)$$

$$f(1)$$

$$\lim_{x \rightarrow 1^+} f(x)$$

$$\lim_{x \rightarrow 1^-} f(x)$$

$$\lim_{x \rightarrow 1} f(x)$$



Example 2:

Using the graph, find the following.

$$f(2)$$

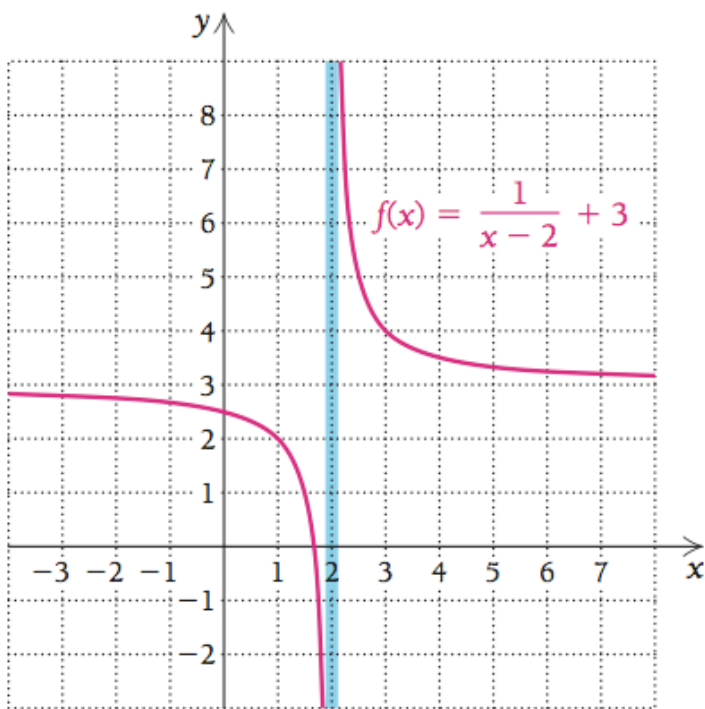
$$\lim_{x \rightarrow 2^+} f(x)$$

$$\lim_{x \rightarrow 2^-} f(x)$$

$$\lim_{x \rightarrow 2} f(x)$$

$$\lim_{x \rightarrow -\infty} f(x)$$

$$\lim_{x \rightarrow +\infty} f(x)$$



Example 3:
Using the graph, find the following.

$$\lim_{x \rightarrow 3} f(x)$$

$$f(2)$$

$$\lim_{x \rightarrow 2^+} f(x)$$

$$\lim_{x \rightarrow 2^-} f(x)$$

$$\lim_{x \rightarrow 2} f(x)$$

$$\lim_{x \rightarrow -\infty} f(x)$$

$$\lim_{x \rightarrow \infty} f(x)$$

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Limits and Graphs

Function Notation $f(x) = x^2 + 3x + 5$

f is the name of the function

f(x) indicates that x is the variable

f(x) is another name for y ~~x~~

f(2) means to plug in 2 for the variable x

$$f(2) = 2^2 + 3(2) + 5 = 4 + 6 + 5 = 15$$

f(2) is the y-value when x-value is 2

the point on the graph is $(2, 15)$

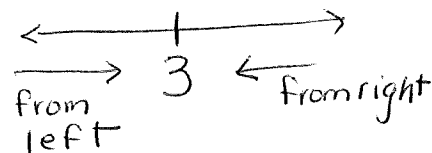
Limit Notation

→ means approaches, gets closer to

$x \rightarrow 3$ means as x approaches 3

$x \rightarrow 3^+$ means as x approaches 3 from the right

$x \rightarrow 3^-$ means as x approaches 3 from the left



Definition

As x approaches a, the limit of f(x) is L written

$$\lim_{x \rightarrow a} f(x) = L$$

If all values of f(x) are close to L for all values of x that are sufficiently close to a. The limit L, if it exists, must be a unique real number.

Theorem

As x approaches a, the limit of f(x) is L if the limit from the left exists and the limit from the right exists and both numbers are equal.

If the right and left limits are not the same, THE limit does not exist (DNE)

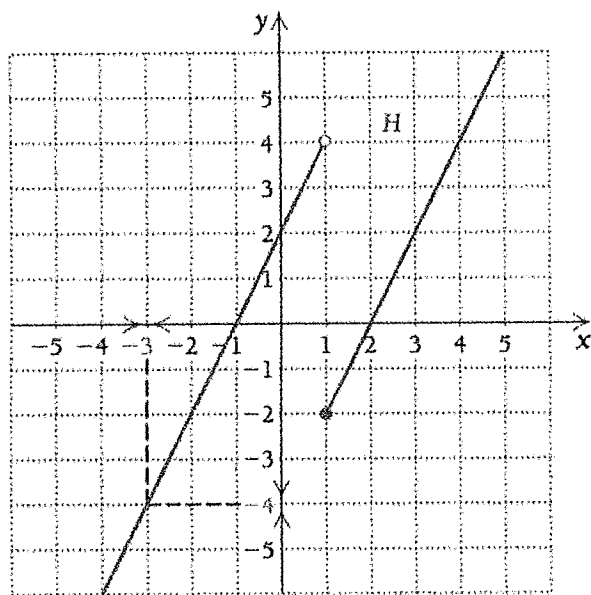
If $f(x)$ is increasing without bound, limit is $+\infty$.

If $f(x)$ is decreasing without bound, limit is $-\infty$.

Limits can also be used to describe behavior on the extreme left and right ends of graph.

$$\lim_{x \rightarrow -\infty} f(x)$$

$$\lim_{x \rightarrow \infty} f(x)$$



Example 1:

Using the graph, find the following.

$$f(-3) = 4$$

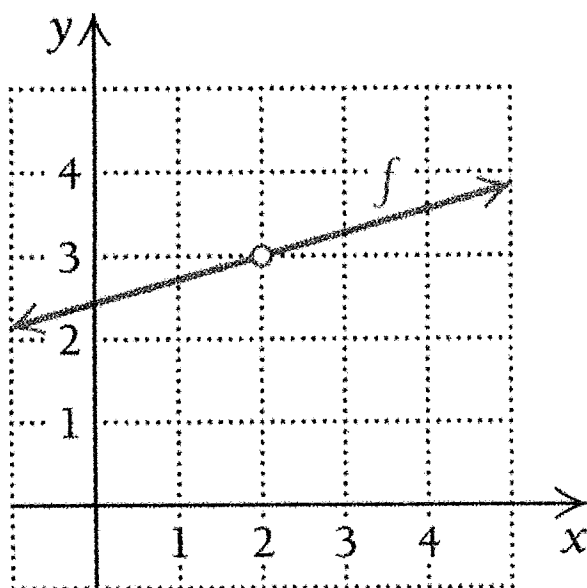
$$f(0) = 2$$

$$f(1) = -2$$

$$\lim_{x \rightarrow 1^+} f(x) = -2$$

$$\lim_{x \rightarrow 1^-} f(x) = 4$$

$$\lim_{x \rightarrow 1} f(x) \text{ Does Not Exist}$$



Example 2:

Using the graph, find the following.

$$f(2) \text{ undefined}$$

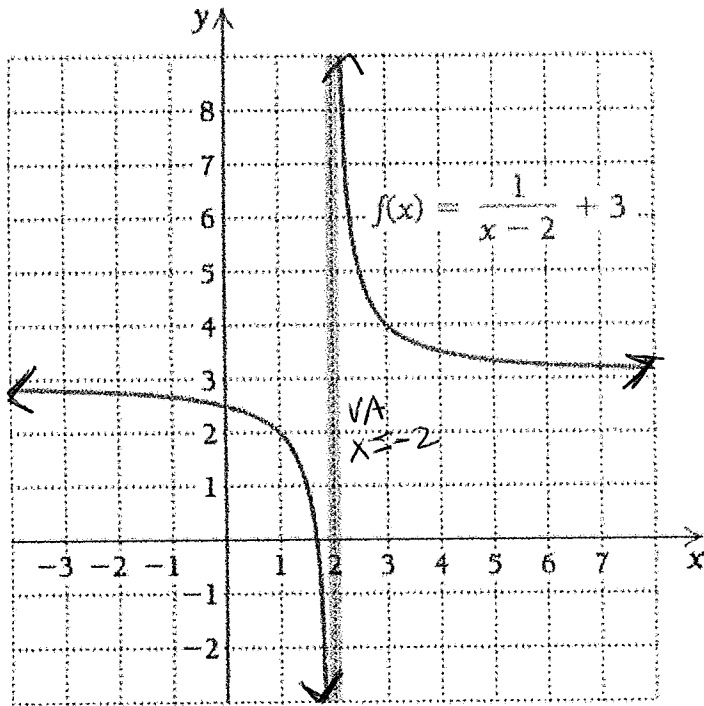
$$\lim_{x \rightarrow 2^+} f(x) = 3$$

$$\lim_{x \rightarrow 2^-} f(x) = 3$$

$$\lim_{x \rightarrow 2} f(x) = 3$$

$$\lim_{x \rightarrow -\infty} f(x) = -\infty$$

$$\lim_{x \rightarrow +\infty} f(x) = +\infty$$



Example 3:

Using the graph, find the following.

$$\lim_{x \rightarrow 3} f(x) = 4$$

$f(2)$ undefined

$$\lim_{x \rightarrow 2^+} f(x) = +\infty$$

$$\lim_{x \rightarrow 2^-} f(x) = -\infty$$

$\lim_{x \rightarrow 2} f(x)$ Does not exist

$$\lim_{x \rightarrow -\infty} f(x) = 3$$

$$\lim_{x \rightarrow \infty} f(x) = 3$$